

$$T = 10 \text{ ms}$$

$$C_0 = 5$$

$$C_1 = 3 + 3j$$

$$C_2 = 2 - j$$

$$C_3 = 0.5 + j$$

$$C_4 = 0.2 - 0.2j$$

$$C_5 = 0.3j$$

$$C_6 = 0.05$$

$$a) \quad H(f) = \begin{cases} (1 - f/600) e^{-j0.02\pi f} & \text{si } |f| \leq 600 \text{ Hz} \\ 0 & \text{si } |f| > 600 \text{ Hz} \end{cases}$$

Sabemos que $\omega_n = \frac{2\pi}{T} \cdot n$ y que $\omega = 2\pi f$

$$\cdot \omega_0 = 0 \Rightarrow C_0 = 5, \quad f_0 = \frac{\omega_0}{2\pi} = \underline{0 \text{ Hz}}$$

$$\cdot \omega_1 = \frac{2\pi}{T}, \quad f_1 = \frac{\omega_1}{2\pi} = \frac{2\pi}{2\pi T} = \frac{1}{T} = \frac{1}{10 \text{ ms}} = \frac{1}{10 \cdot 10^{-3} \text{ s}} = \underline{100 \text{ Hz}}$$

$$\cdot \omega_2 = \frac{2\pi}{T} \cdot 2, \quad f_2 = \frac{\omega_2}{2\pi} = \frac{2\pi \cdot 2}{2\pi} \cdot \frac{1}{T} = \frac{2}{T} = \frac{2}{10^{-2}} \text{ Hz} = \underline{200 \text{ Hz}}$$

$$\cdot \omega_3 = \frac{2\pi}{T} \cdot 3, \quad f_3 = \frac{\omega_3}{2\pi} = \frac{2\pi \cdot 3}{2\pi} \cdot \frac{1}{T} = \frac{3}{T} = \underline{300 \text{ Hz}}$$

$$\cdot \omega_4 = \frac{2\pi}{T} \cdot 4, \quad f_4 = \frac{\omega_4}{2\pi} = \frac{2\pi \cdot 4}{2\pi} \cdot \frac{1}{T} = \frac{4}{T} = \underline{400 \text{ Hz}}$$

$$\cdot \omega_5 = \frac{2\pi}{T} \cdot 5, \quad f_5 = \frac{\omega_5}{2\pi} = \frac{2\pi \cdot 5}{2\pi} \cdot \frac{1}{T} = \frac{5}{T} = \underline{500 \text{ Hz}}$$

$$\cdot \omega_6 = \frac{2\pi}{T} \cdot 6, \quad f_6 = \frac{\omega_6}{2\pi} = \frac{2\pi \cdot 6}{2\pi} \cdot \frac{1}{T} = \frac{6}{T} = \underline{600 \text{ Hz}}$$

• Calculemos los coeficientes despues de pasar por el sistema

$$\cdot \boxed{C_0'} = C_0 \cdot H(0) = C_0 = \boxed{5}$$

$$H(0) = \left(1 - \frac{0}{600}\right) e^{+0} = 1$$

$$\cdot C_1' = C_1 \cdot H(100)$$

$$H(100) = \left(1 - \frac{100}{600}\right) \cdot e^{-j \cdot 0.02 \cdot \pi \cdot 100} = \frac{5}{6} e^{-j\pi 2}$$

$$\begin{aligned} \boxed{C_1'} &= C_1 \cdot \frac{5}{6} e^{-j\pi 2} = \frac{5}{6} C_1 \cdot (\cos(-2\pi) + j \cdot \sin(-2\pi)) = \\ &= \frac{5}{6} C_1 = \frac{5}{6} \cdot (3 + 3j) = \boxed{\frac{5}{2} + \frac{5}{2}j} \end{aligned}$$

$$\cdot C_2' = C_2 \cdot H(200)$$

$$H(200) = \left(1 - \frac{200}{600}\right) e^{-j \cdot 0.02 \cdot \pi \cdot 200} = \frac{2}{3} e^{-j4\pi}$$

$$\begin{aligned} \boxed{C_2'} &= C_2 \cdot \frac{2}{3} e^{-j4\pi} = \frac{2}{3} C_2 \cdot (\cos(-4\pi) + j \cdot \sin(-4\pi)) = \frac{2}{3} C_2 = \\ &= \frac{2}{3} (2 - j) = \boxed{\frac{4}{3} - \frac{2}{3}j} \end{aligned}$$

$$C_3' = C_3 \cdot H(300)$$

$$H(300) = \left(1 - \frac{300}{600}\right) e^{-j \cdot 0.02 \cdot \pi \cdot 300} = \frac{1}{2} e^{-j6\pi}$$

$$\begin{aligned} \boxed{C_3'} &= C_3 \cdot \frac{1}{2} e^{-j6\pi} = \frac{1}{2} C_3 (\cos(-6\pi) + j \cdot \sin(-6\pi)) = \frac{1}{2} C_3 = \\ &= \frac{1}{2} (0.5 + j) = \boxed{\frac{1}{4} + \frac{1}{2}j} \end{aligned}$$

$$C_4' = C_4 \cdot H(400)$$

$$H(400) = \left(1 - \frac{400}{600}\right) e^{-j0.02\pi \cdot 400} = \left(1 - \frac{2}{3}\right) e^{-j8\pi} = \frac{1}{3} e^{-j8\pi}$$

$$C_4' = C_4 \cdot \frac{1}{3} e^{-j8\pi} = \frac{1}{3} C_4 \cdot (\cos(-8\pi) + j \cdot \sin(-8\pi)) = \frac{1}{3} C_4$$

$$\boxed{C_4' = \frac{1}{3} (0.2 - 0.2j) = \frac{2}{30} - \frac{2}{30}j}$$

$$C_5' = C_5 \cdot H(500)$$

$$H(500) = \left(1 - \frac{500}{600}\right) e^{-j0.02\pi \cdot 500} = \frac{1}{6} e^{-j10\pi}$$

$$\boxed{C_5' = C_5 \cdot \frac{1}{6} e^{-j10\pi} = \frac{1}{6} C_5 = \frac{1}{6} (0.3j) = \frac{3}{60} j = \frac{1}{20} j}$$

$$C_6' = C_6 \cdot H(600)$$

$$H(600) = \left(1 - \frac{600}{600}\right) e^{-j0.02\pi \cdot 600} = 0$$

$$\boxed{C_6' = C_6 \cdot 0 = 0}$$

- Determinar la señal resultante en el dominio del tiempo.

$$g(t) = \frac{1}{T} \sum_{-\infty}^{\infty} C_n' e^{j\omega_n t}$$

C_n' para $|n| \geq 6$ es $C_n' = 0$ pues $H(f) = 0$ para esos $|f| > 600$ Hz.
entonces nos queda

$$g(t) = \frac{1}{T} \sum_{-5}^5 C_n' e^{j\omega_n t}$$

$$C_{-1}' = \overline{C_1'} = (\text{conjugado}) = \frac{5}{2} - \frac{5}{2}j$$

$$C_{-3}' = \overline{C_3'} = \frac{1}{4} - \frac{1}{2}j$$

$$C_{-2}' = \overline{C_2'} = \frac{4}{3} + \frac{2}{3}j$$

$$C_{-4}' = \overline{C_4'} = \frac{2}{30} + \frac{2}{30}j$$

$$C_{-5}' = \overline{C_5'} = -\frac{1}{20}j$$

$$g(t) = \frac{1}{T} \sum_{-5}^5 c_n' e^{j\omega_n t}$$

$$\omega_0 = 0$$

$$\omega_1 = \frac{2\pi}{T} = \frac{2\pi}{10^{-2}} = 2\pi \cdot 100 \text{ rad/s} = 200\pi \text{ rad/s}$$

$$\omega_2 = \frac{4\pi}{T} = \frac{4\pi}{10 \cdot 10^{-3}} = 400\pi \text{ rad/s}$$

$$\omega_3 = \frac{6\pi}{T} = 600\pi \text{ rad/s}$$

$$\omega_4 = \frac{8\pi}{T} = 800\pi \text{ rad/s}$$

$$\omega_5 = 1000\pi \text{ rad/s}$$

$$g(t) = \frac{1}{10^{-2}} \cdot (c_{-5}' e^{-j \cdot 1000\pi t} + \dots + c_5' \cdot e^{j1000\pi t})$$

-Distorsiones

• Hay distorsión de atenuación, veamos por qué:

$$H(f) = \left(1 - \frac{f}{600}\right) e^{-j \frac{2}{100} \pi f} \quad \text{para } |f| \leq 600 \text{ Hz. (donde están presentes armónicos)}$$

$$H(f) = \left(1 - \frac{f}{600}\right) \cdot \left(\cos\left(-\frac{2\pi f}{100}\right) + j \cdot \sin\left(-\frac{2\pi f}{100}\right)\right)$$

$$|H(f)|_{\text{modulo}} = \sqrt{\left(1 - \frac{f}{600}\right)^2 \cdot \left(\underbrace{\cos^2\left(\frac{-2\pi f}{100}\right) + \sin^2\left(\frac{-2\pi f}{100}\right)}_1\right)} = 1 - \frac{f}{600}$$

$$|H(f)| = 1 - \frac{f}{600} \quad \text{si } |f| \leq 600 \text{ Hz. Hay distorsión de atenuación porque}$$

$|H(f)|$ no es constante para toda frecuencia. $|f| \leq 600 \text{ Hz}$ y cada armónico cambia de forma diferente.

• Calculamos ahora la fase:

$$\phi(f) = \operatorname{arctg} \left(\frac{-\sin\left(-\frac{2\pi f}{100}\right)}{\cos\left(-\frac{2\pi f}{100}\right)} \right) = \operatorname{arctg} \left(-\operatorname{tg}\left(-\frac{2\pi f}{100}\right) \right) = \operatorname{arctg} \left(\operatorname{tg}\left(\frac{2\pi f}{100}\right) \right) =$$

No hay distorsión de retardo porque la fase es lineal. $= \frac{2\pi f}{100}$

b) El A.B del medio de transmisión, es decir, de su función de transferencia es

$\omega_0 = \frac{1}{RC} = 100\pi \text{ rad/s}$. Como todos los armónicos de la señal son de frecuencia mucho mayor que el A.B esto implica que no se transmitirá correctamente.